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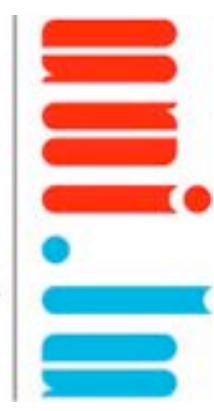


# Machine Learning of Molecular Quantum Chemical Space *Opportunities and Challenges*

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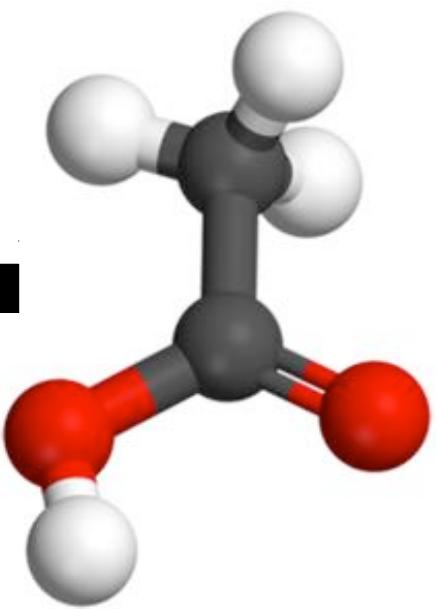


UNIVERSITÉ DU  
LUXEMBOURG



NeurIPS, December 8, 2018

# Quantum physics/chemistry today



$$\text{DFT} \quad \hat{\mathcal{H}}(R_1, Z_1, \dots, R_N, Z_N) \tilde{\Psi} = E \tilde{\Psi}$$

MP2  
CCSD(T)  
...



Properties: Energy, polarizability, HOMO, LUMO, ...  
Dynamics: Thermal properties, spectroscopy, ...

# Quantum physics/chemistry tomorrow?

ML  
Insights:

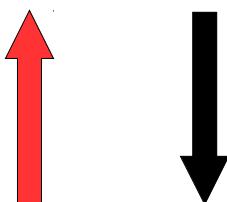
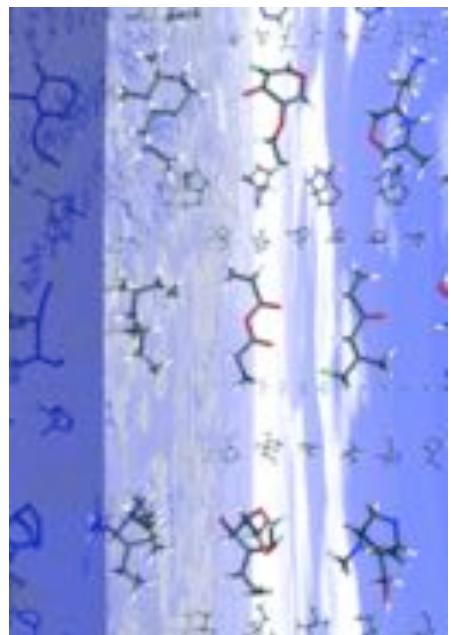
- Structure of chemical space

- Reactivity trends,

- aromaticity,  
“new” chemistry

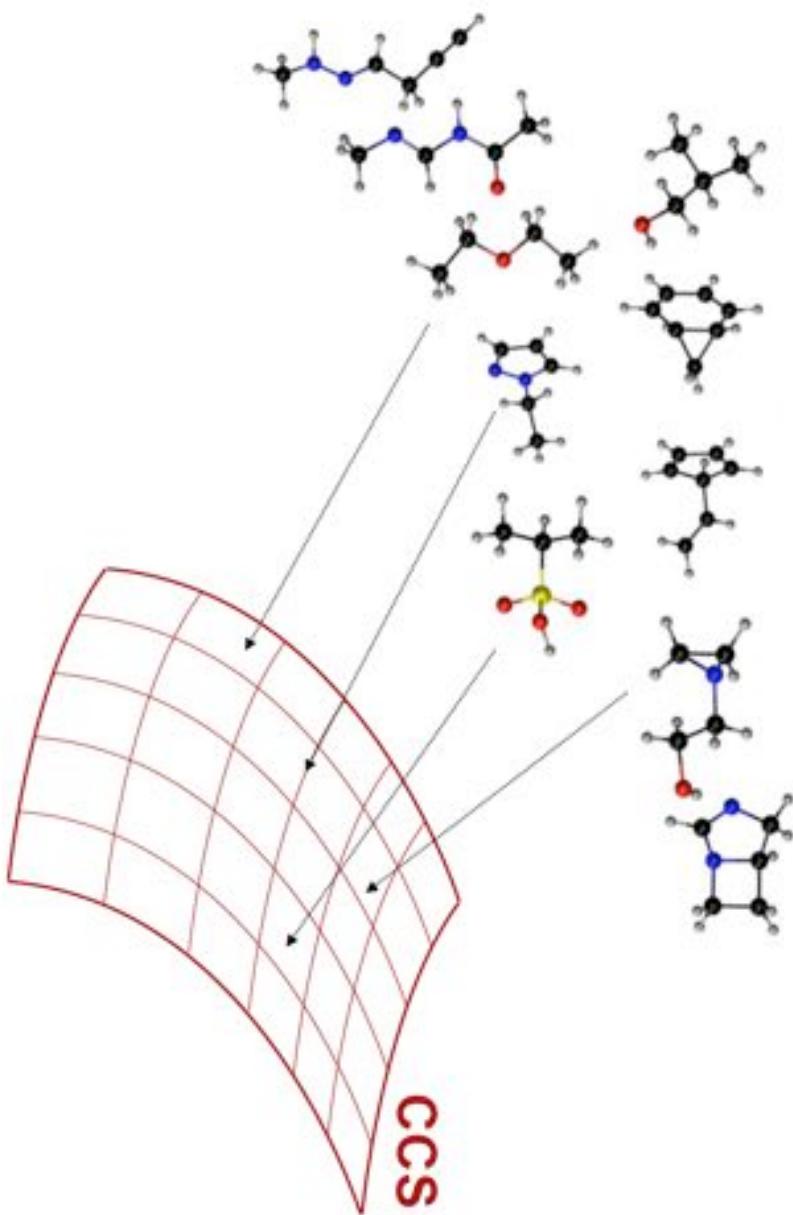
- Molecular design through multi-property optimization

- ...



Training data:  
molecular properties

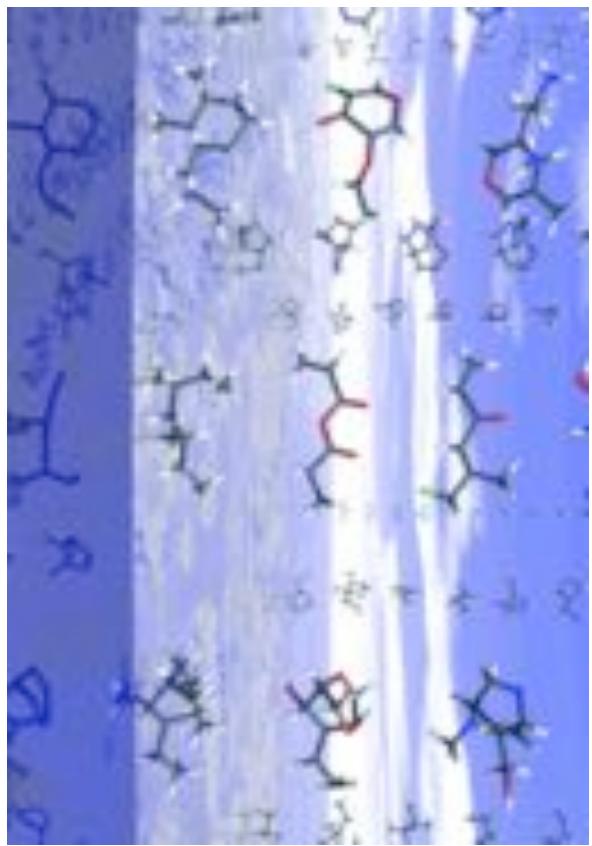
# Molecular Quantum Chemical Space



$\{R_i, Z_i\}$  maps to  $\{P_1, P_2, P_3, P_4, \dots\}$

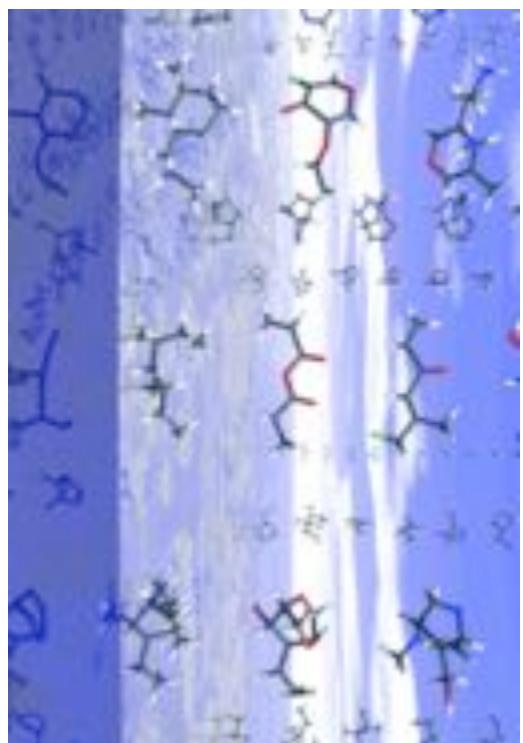
- Graph theory:  
combinatorial explosion
- At least  $10^{60}$  small drug  
candidate molecules
- Finding needles in a  
haystack

# Machine learning for molecular big data



- **Descriptor:** what's a good representation of a molecule?
  - **Metric:** how to define distance between two molecules?
  - **Data selection:** Which molecules to use for training?
  - **Properties:** which set of properties uniquely defines a molecule?
  - **Degrees of freedom:** composition vs. conformation
- $\{R_i, Z_i\}$  maps to  $\{P_1, P_2, P_3, P_4, \dots\}$

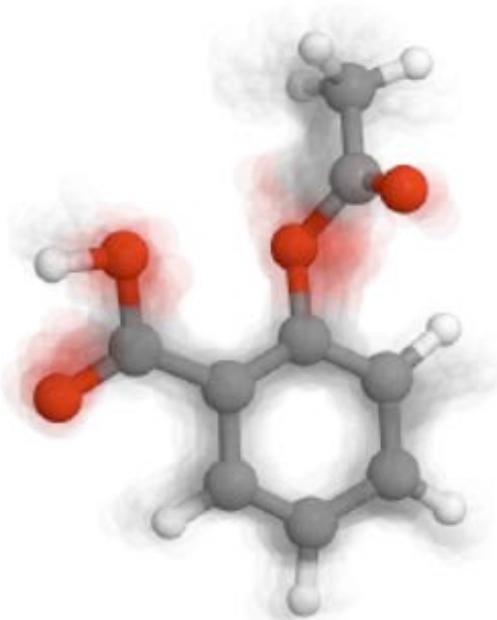
# Molecular Data in this Talk



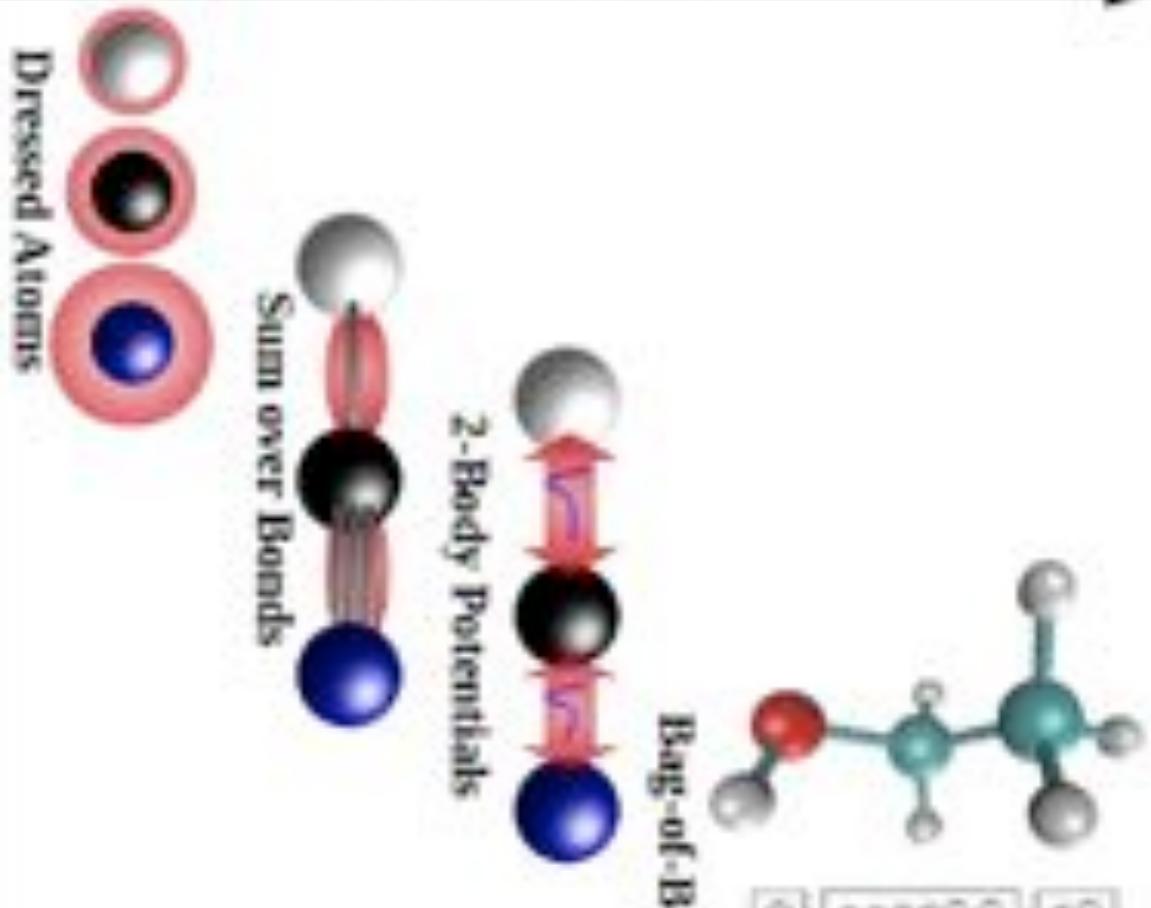
**GDB mol graphs:** J. L. Reymond (U. Bern)  
<http://gdb.unibe.ch/downloads/>

**QM7/QM9 datasets:** Hybrid DFT calculations by **von Lilienfeld's** group (Sci. Data 2014) and my group (PRL 2012).

**MD17/ISO17 datasets:** Molecular dynamics trajectories from my group (DFT and CCSD(T) levels)



# Predicting Molecular Properties: The Importance of *Physical Baselines*



K. Hansen, F. Biegler,  
R. Ramakrishnan, W. Pronobis,  
O. A. von Lilienfeld,  
K.-R. Mueller, and A. Tkatchenko,  
*J. Phys. Chem. Lett.* 6, 2326 (2015).

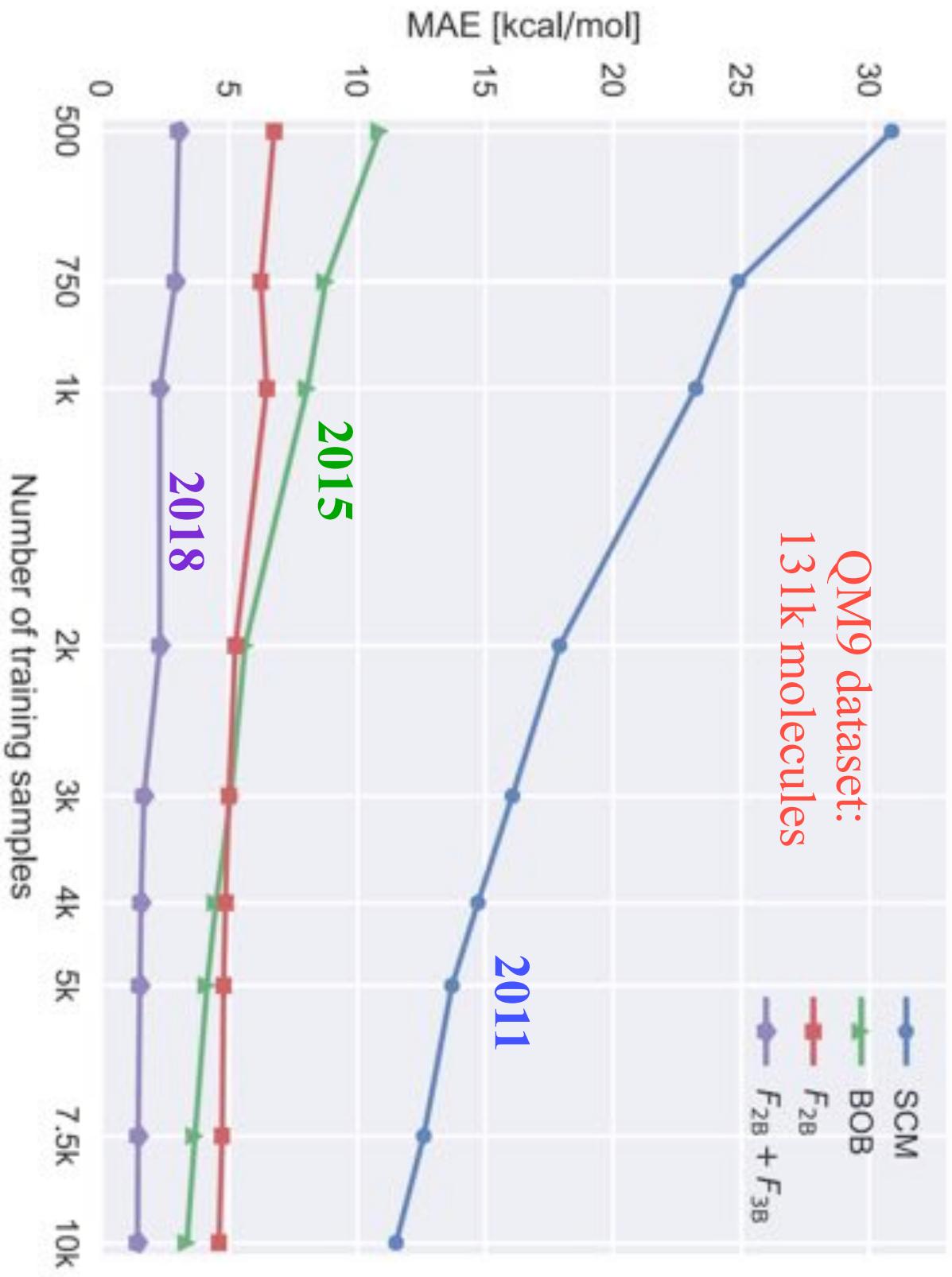
# Predicting Molecular Properties: QM7 dataset

model	MAE [kcal/mol]
dressed atoms	15.1
sum-overbonds	9.9
Lennard-Jones potential	8.7
polynomial pot. ( $n = 6$ )	5.6
polynomial pot. ( $n = 10$ )	3.9
polynomial pot. ( $n = 18$ )	3.0
Bag of Bonds ( $p = 2$ , Gaussian)	4.5
Bag of Bonds ( $p = 1$ , Laplacian)	1.5
Coulomb matrix ( $p = 2$ , Gaussian) <sup>17</sup>	10.0
Coulomb matrix ( $p = 1$ , Laplacian) <sup>16</sup>	4.3

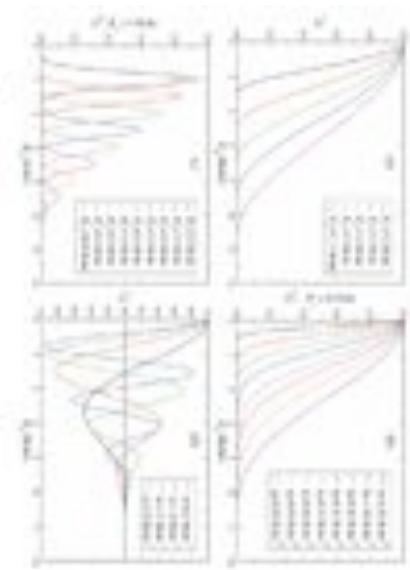
**2+3body many-body expansion**

**0.8**

# QM9 dataset: Evolution from Coulomb Matrix to Many-Body Representation



# Zoo of Descriptors for Molecules and Solids



$$M_{ij} = \begin{cases} 0.5Z_i^{2.4} & \text{for } i = j \\ \frac{Z_i Z_j}{d_{ij}} & \text{for } i \neq j \end{cases}$$

Coulomb matrix  
(Rupp et al. 2012)

Bag of bonds  
(Hansen et al. 2015)

Atom-centered  
symmetry functions  
(Behler et al. 2007)

$\{Z_i, \mathbf{R}_i\}$

$\{Z_i, d_{ij}\}$

$$k(\rho, \rho') = \int d\hat{R} \left| \rho(\mathbf{r}) \rho'(\hat{R}\mathbf{r}) \right|^n$$

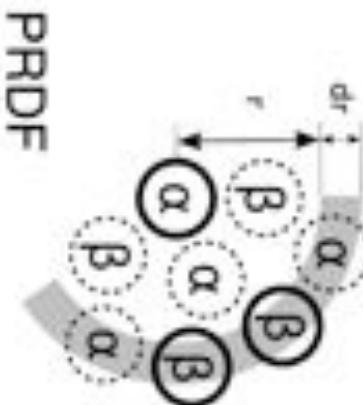
SOAP

(Bartók et al. 2013)

$$x_{ij} = \begin{cases} 0.5Z_i^{2.4} & \text{if } i = j \\ \frac{Z_i Z_j}{\phi(r_i, r_j)} & \text{if } i \neq j \end{cases}$$

Sine matrix

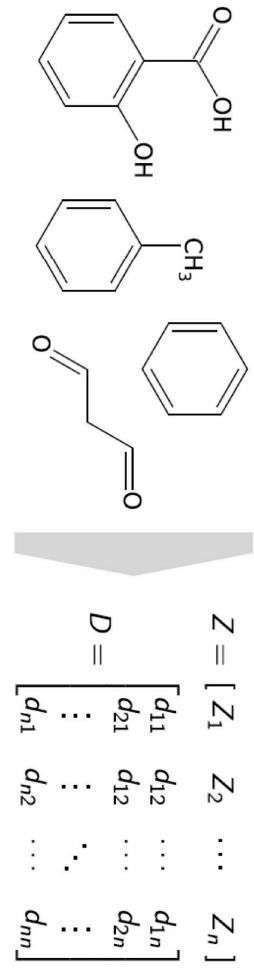
(Faber et al. 2015)



PRDF  
(Schütt et al, 2014)

# Learning the Representation: Deep Tensor Neural Networks (DTNN)

**Input:** Atomic numbers and interatomic distances



**Embedding of based on atom types**

$$\mathbf{x}_i^{(0)} = \mathbf{x}_{Z_i} \in \mathbb{R}^d$$

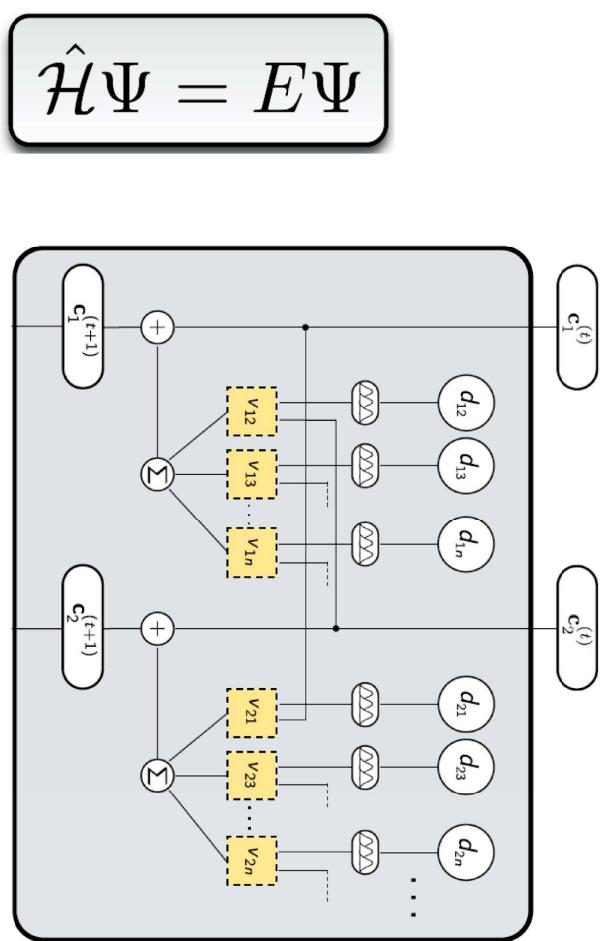
**Add interaction with environment using  $t = 1 \dots T$**   
**sequential refinements  $\mathbf{v}_i^{(t)}$**

$$\mathbf{x}_i^{(t+1)} = \mathbf{x}_i^{(t)} + \mathbf{v}_i^{(t)} \left( \mathbf{x}_1^{(t)}, \dots, \mathbf{x}_{n_{\text{atoms}}}^{(t)}, d_{i1}, \dots, d_{in_{\text{atoms}}} \right)$$

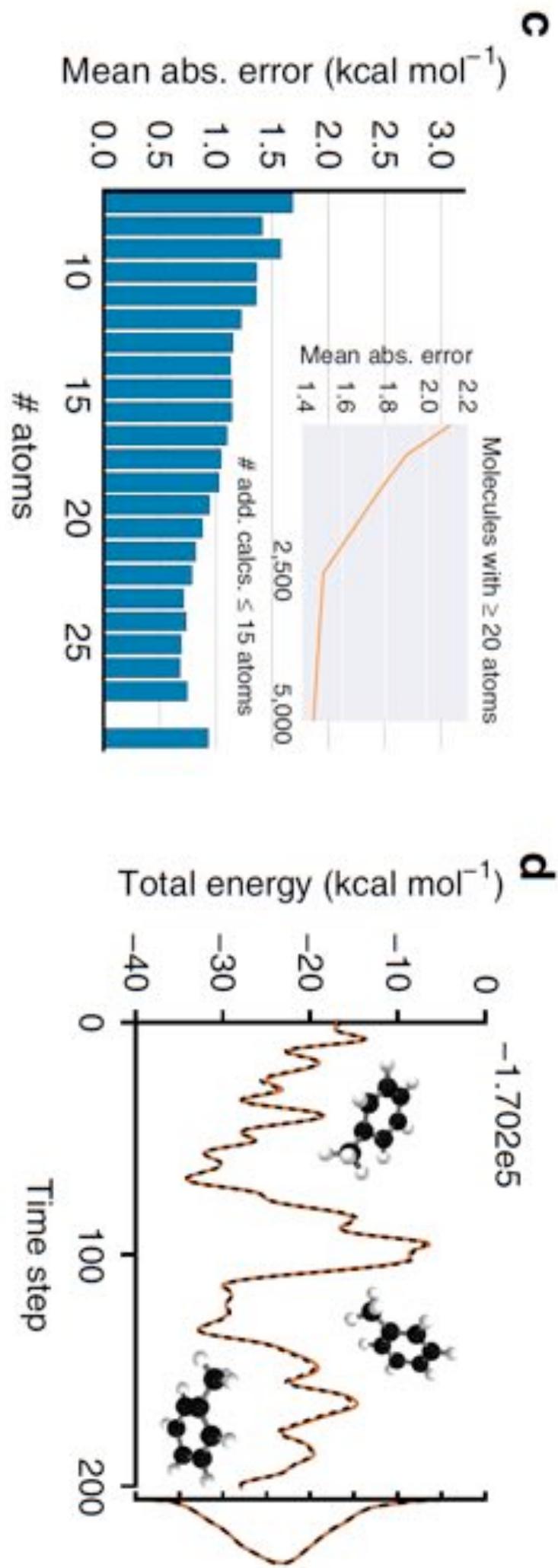
**Prediction via atom-wise contributions:**

$$\hat{E} = \sum_{i=1}^{n_{\text{atoms}}} f_{\text{out}}(\mathbf{x}_i^{(T)})$$

Mean absolute error on QM9: **0.2 kcal/mol**



# Learning Full Chemical Space with DTNN?



Accurately representing **BOTH** compositional and conformational degrees of freedom is difficult.

For C<sub>7</sub>O<sub>2</sub>H<sub>10</sub> isomer and MD data, the error grows to > 1.0 kcal/mol

# Beating the Hell out of Data: Gradient-Domain Machine Learning (GDML)

B Energy domain



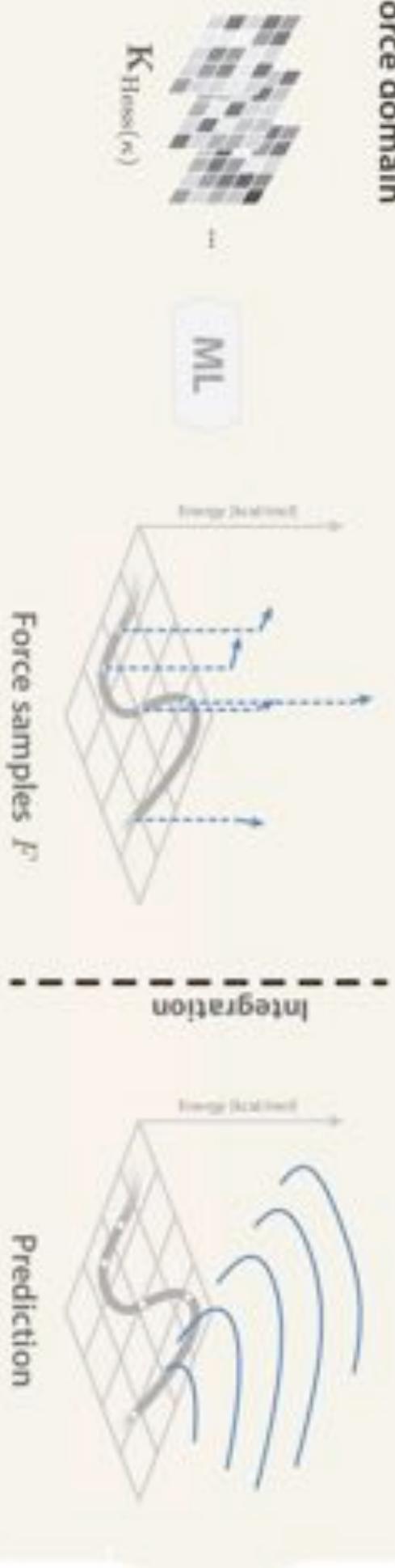
Kernel



Energy samples  $V_{BG}$

Prediction

C Force domain



Force samples  $F$

Prediction

$K_{Hess}(\kappa)$

ML

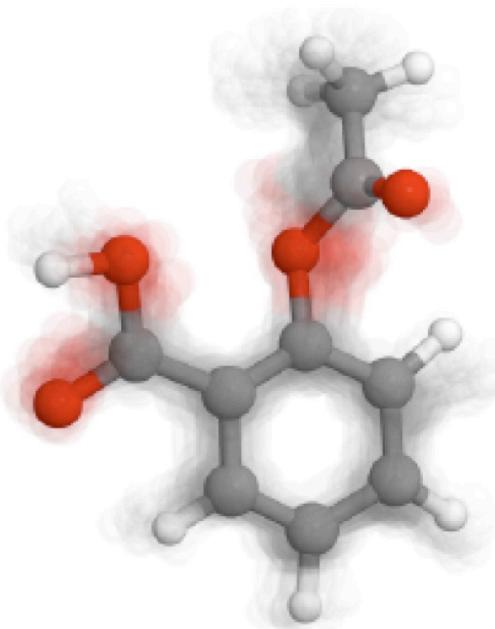
Energy (scaled)

Integration

Energy (scaled)

S. Chmiela, A. Tkatchenko, H. Sauceda, I. Poltavsky, K. T. Schuett, K.-R. Mueller,  
*Science Adv.* 3, e1603015 (2017).

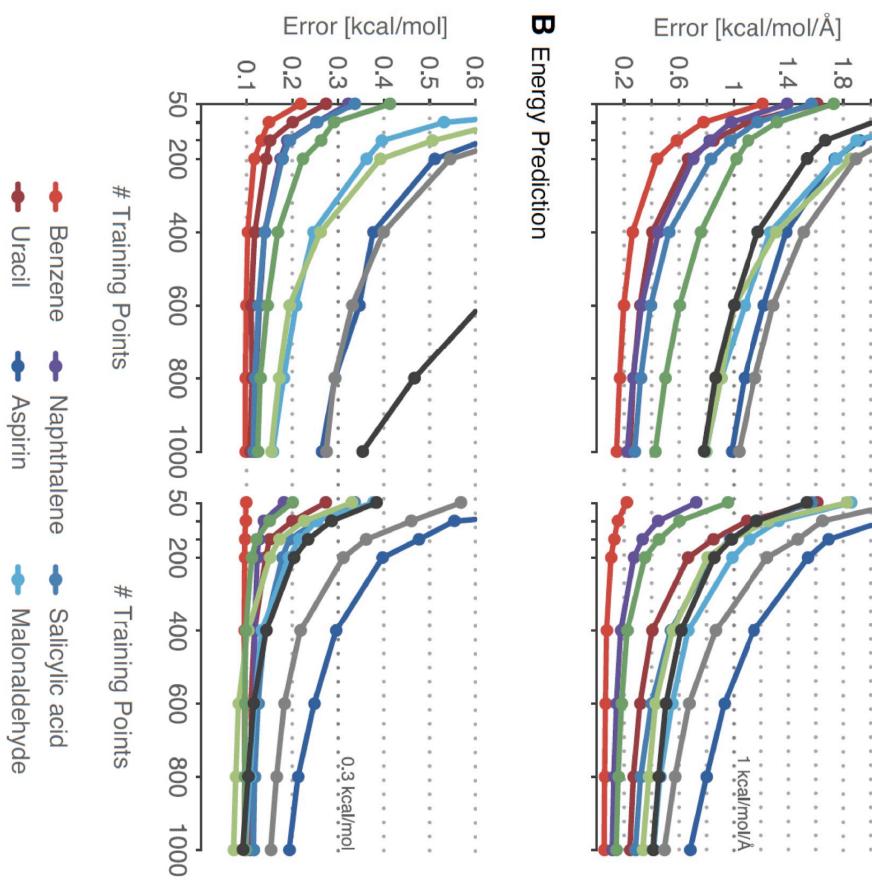
# Symmetrized Gradient-Domain Machine Learning: Towards Exact Molecular Force Fields



**A** Force Prediction

Model Convergence

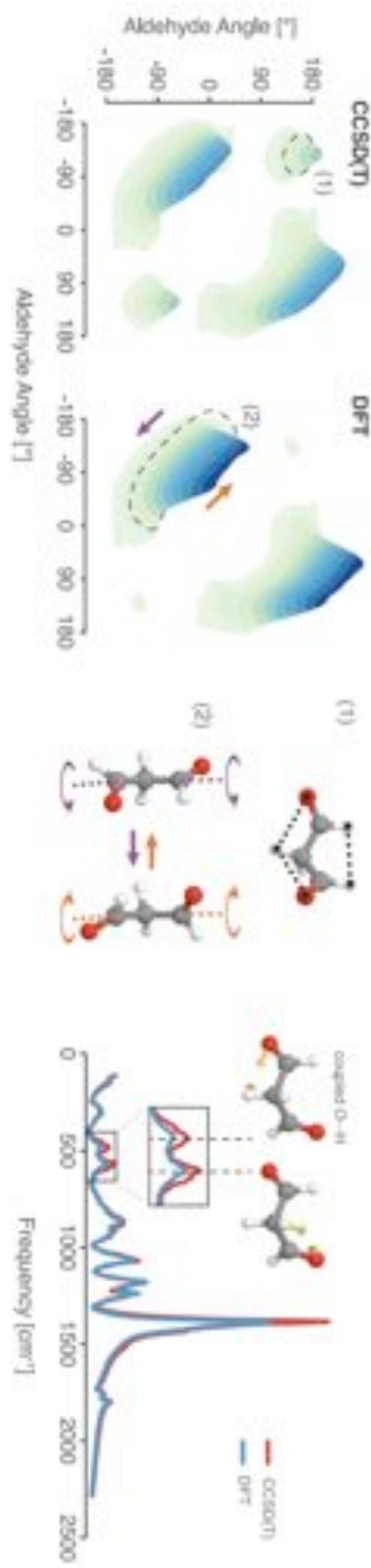
**B** Energy Prediction



Globally accurate force field from only 100s of conformations

# Embarrassingly Quantum MD for Molecules: Quantized Electrons [CCSD(T)] and Nuclei [PIMD]

**A** Malonalsalicylate Probability Distribution & Vibrational Spectrum

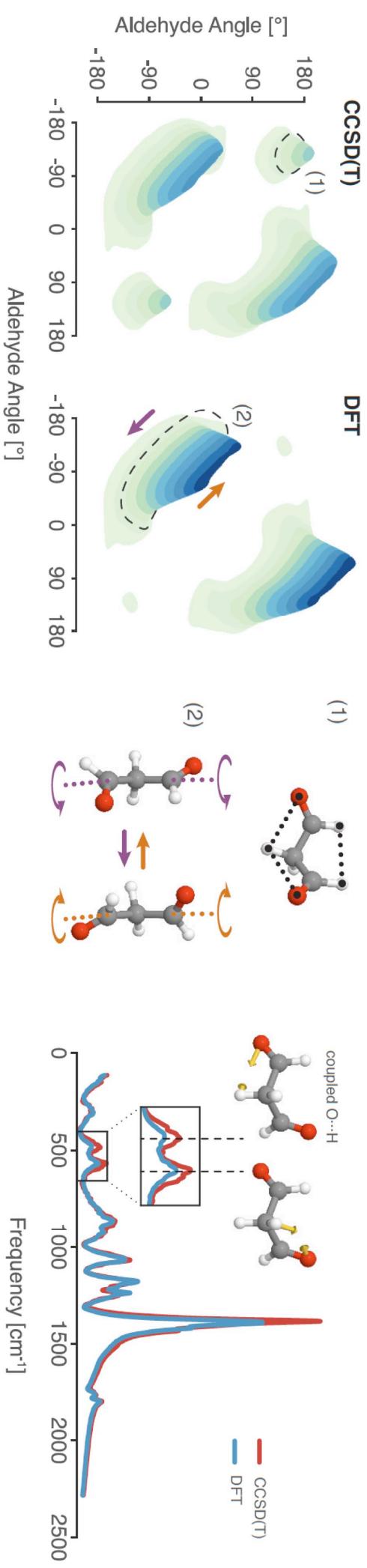


S. Chmiela, H. Sauceda, K.-R. Mueller, and A. Tkatchenko

*Nature Commun.* 9, 3887 (2018).

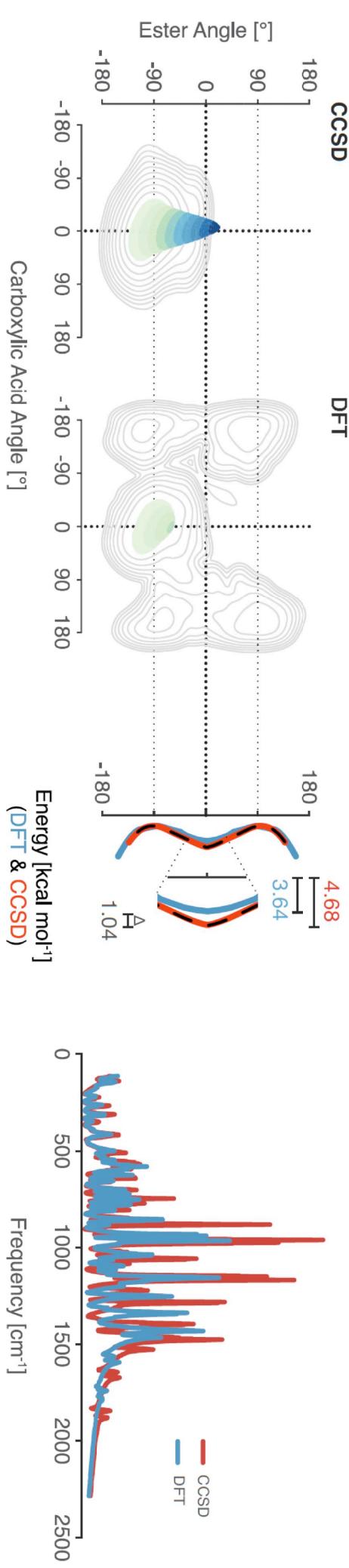
# Embarrassingly Quantum MD for Molecules: Quantized Electrons [CCSD(T)] and Nuclei [PiMD]

**A** Malonaldehyde Probability Distribution & Vibrational Spectrum



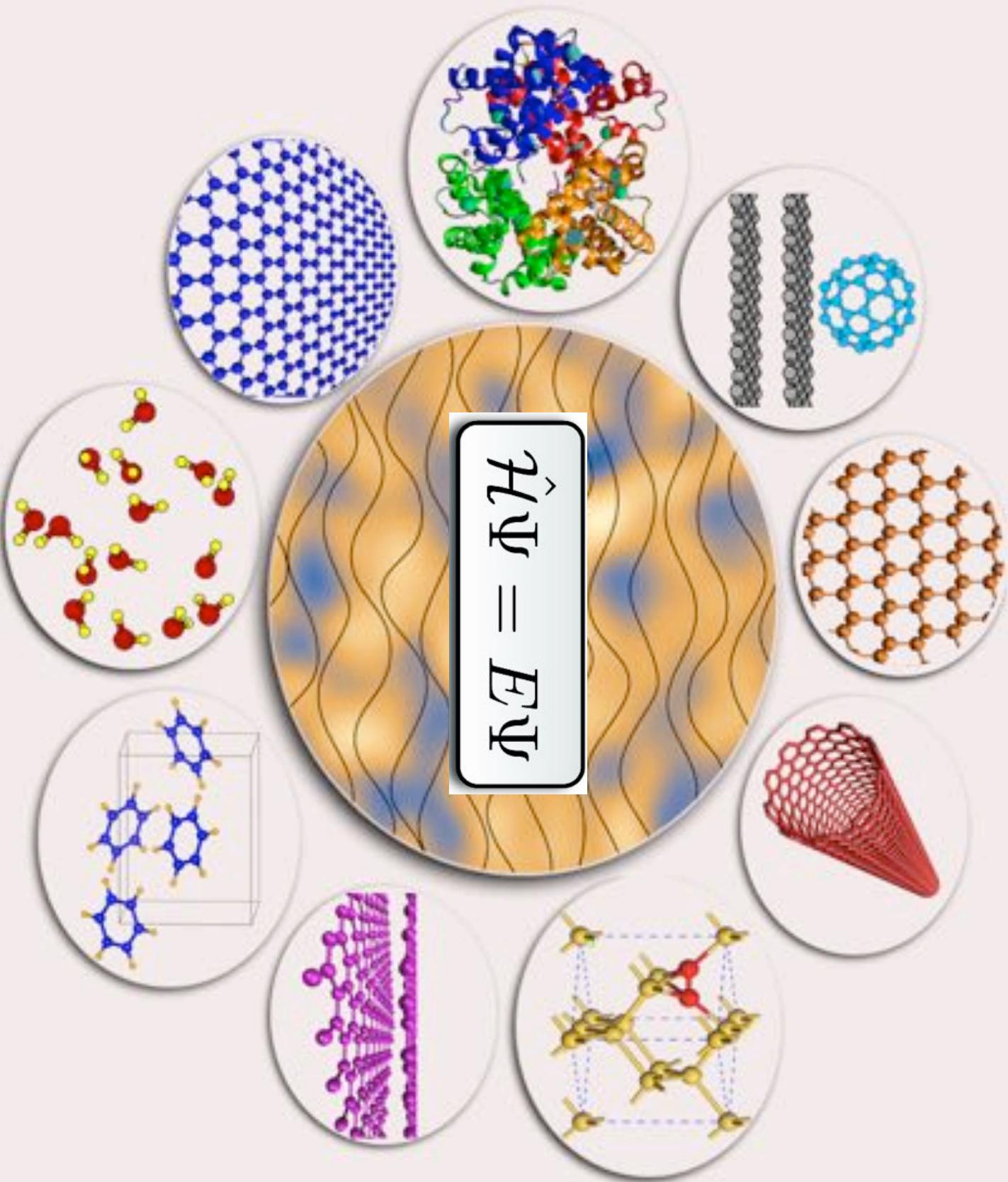
**B** Aspirin Probability Distribution & Vibrational Spectrum

\* The sGML model for aspirin was trained on CCSD reference data.



S. Chmiela, H. Sauceda, K.-R. Mueller, and A. Tkatchenko

*Nature Commun.* 9, 3887 (2018).



# Grand Challenges for Machine Learning in Physics/Chemistry

- *What is chemical space:* descriptors of molecules and materials, metric?
- *How to learn intensive properties:* energy levels, excited states, spectra?
- How to combine ML with physical laws (symmetries) and interaction models?
- Can we learn (approximate) Hamiltonians?
- Can ML suggest better approximations for  $\hat{\mathcal{H}}\Psi = E\Psi$  ?
- More and better (big) data

*Towards rational design of molecules and materials in  
chemical space*